# Zillions of Practice Problems for Beginning Algebra

Stanley F. Schmidt, Ph.D.



Polka Dot Publishing

### What This Book Is All About

n the Life of Fred: Beginning Algebra Expanded Edition book, there are Your Turn to Play sections after each topic is presented. And each Your Turn to Play offers complete solutions to each question.

At the end of each chapter are three problem sets, each named after a city. Each of the problems in these cities is also completely worked out in the book.

I thought that all those problems would be enough. I still think all those problems are enough. As they say in German: *Genug ist genug.*\*

(4) (4) (4)

*Some* of my readers have written to me, "Enough is not enough. We want more. We want tons of problems along with completely worked out solutions. We need the drill-and-kill approach. My kids are not crying when they read Fred—how could they be learning math without crying?"

If you are a part of those *some readers*, then this *Zillions of Practice Problems* was written for you.

#### HOW THIS BOOK IS ORGANIZED

Life of Fred: Beginning Algebra Expanded Edition is in twelve chapters. This book also has twelve chapters.

As you work through each chapter in *Life of Fred: Beginning Algebra Expanded Edition*, you can do as many of the problems as you like in the corresponding chapter in this book.

<sup>\* &</sup>quot;Enough is enough." I learned this nifty phrase when I studied German in high school.

#### CHAPTERS IN THIS BOOK

Each chapter in this book is divided into two parts.

- \* The first part takes each topic and offers a zillion problems.
- \* The second part is called the Mixed Bag. It consists of a variety of problems from the chapter and review problems from the beginning of the book up to that point.

#### COMPLETE SOLUTIONS

Every problem (gasp!) will receive a detailed solution—not just the answer.

#### ELIMINATING TEMPTATION

The solutions and answers are all given in the back half of the book. The first question in this book is numbered "45." The second one is "888." In most ordinary practice books, they are numbered, "1, 2, 3 . . ." which is really silly when you think about it. In those books, when you look up the answer to "1" you might accidentally see the answer to "2" and that would spoil all the fun.

# Contents

Chapter 1	Numbers and Sets. 11 finite and infinite sets natural numbers, whole numbers, integers set notation negative numbers ratios the empty set
Chapter 2	The Integers
Chapter 3	Equations
Chapter 4	Motion and Mixture
Chapter 5	Two Unknowns
Chapter 6	Exponents

Cnapter /	multiplying binomials and trinomials polynomials first kind of factoring: common factors factoring easy trinomials: x² + bx + c factoring a difference of squares factoring by grouping factoring harder trinomials: ax² + bx + c solving quadratic equations by factoring
Chapter 8	Fractions
Chapter 9	Square Roots
Chapter 10	Quadratic Equations
Chapter 11	Functions and Slope
Chapter 12	Inequalities and Absolute Value
	ers worked out in complete detail

#### Chapter Four

#### **Mixture Problems**

6179. Joe wants to make 30 pounds of chili seasoning that contains 30% cayenne pepper. He has one sack of mild chili seasoning that is 10% cayenne and one sack of hot chili seasoning that is 40% cayenne.

How much of each sack should he use?

6704. Darlene has some pancake mix that contains 2% sugar. She calls that her bitter mix. She has some that contains 5% sugar. She calls that her too-sweet mix.

She wants to make 60 pounds of pancake mix that has 3% sugar. How much of each mix should she use?

8975. You are a veterinarian and you need to give a marten a shot to ease its pain. You need to give it 9 cc that contains 6% morphine. You have some 4% and some 10%. How much of each should you mix together?

should you mix together?

(Side note: It is often nice in medical work to get the mathematics right. Too little pain killer and the marten remains in pain. Too much morphine and the martin will look like:

dead marten

201. We need to ship 600 cars to Freedonia, and the order specifies that 28% of those cars should have tape players.

40% of the older cars have tape players, and 15% of the newer cars do. How many older cars should we ship?

1850. Darlene has weak dishwashing liquid that contains 17% soap. She also has strong dishwashing liquid that contains 37% soap.

Darlene just purchased a dishwashing robot. When she read the directions, she found out that the robot would only work if you gave it 444 ounces of dishwashing liquid that contained 22% soap.

How much of each dishwashing liquid should Darlene use?

(Joe never washes his dishes because he only uses paper plates.)



#### Chapter Four

# Second part: the Mixed Bag: a variety of problems from this chapter and previous material

2226. Joe likes his cereal with exactly 8% flour in it. (The rest is sugar and artificial flavorings.) He asked Darlene take his two boxes of cereal—Captain Mousebait (7% flour) and Sergeant Sugar (11% flour)—and mix them together to

get 300 ounces.

How much of each cereal should Darlene use?

1928. Haydn wrote the "Sun" quartets five times as long ago as Robert Frost wrote "In the Clearing."

Sixteen years from now, the "Sun" quartets will be four times as old as "In the Clearing."

How old is "In the Clearing" today?

2258. Joe decided one night to read "In the Clearing." He first read the poem at the rate of 40 words/minute. Then he decided to read it backwards. Reading backwards slowed his reading rate down to 5 words/minute.

It took him a total of 27 minutes to read the poem in both directions. How long did it take Joe to read the poem in the normal direction?

2280. Joe liked to eat jelly beans while he watched television every evening. He bought red jelly beans at a cost of \$5/lb. He bought green jelly beans at \$6/lb. He spent a total of \$488. He bought 8 more pounds of the green than of the red. How many pounds of red jelly beans did he buy?

4507. This particular cat likes some bones in his fish. (It's a good source of calcium.) This cat prefers a fish mixture with 7% bones.

How many pounds of 5% bones should he mix with 8% bones to obtain 36 pounds of fish with 7% bones?

## Chapter Five

#### First part: Problems on Each Topic

#### Solving Two Equations, Two Unknowns by Elimination

1891. Solve 
$$\begin{cases} 7x + 3y = 43 \\ 4x - 3y = 1 \end{cases}$$
2292. Solve 
$$\begin{cases} 5x + 3y = 18 \\ -5x - 10y = 10 \end{cases}$$
2904. Solve 
$$\begin{cases} 10x + 6y = 62 \\ 8x - 2y = 2 \end{cases}$$
4010. Solve 
$$\begin{cases} 4x + 3y = 3 \\ 12x - 7y = -71 \end{cases}$$
4505. Solve 
$$\begin{cases} 6x + 6y = -18 \\ 7x + 8y = -25 \end{cases}$$
4519. Solve 
$$\begin{cases} 6x + 3y = 6 \\ 9x + 10y = 42 \end{cases}$$

#### Union of Sets

- 3328. What is the union of  $\{3, 4, 5\}$  and  $\{4, \heartsuit, w\}$ ?
- 4280.  $\{8\} \cup \{1,2\} = ?$
- 4500.  $\{x \mid x \text{ is an integer and } x > 4\} \cup \{y \mid y \text{ is a whole number and } y < 6\}$
- 600.  $\{1, 2, 3\} \cup \{3, 2, 1\}$
- 800.  $\{ \} \cup \{ \$ \}$
- 924. For any set A, it is always true that  $A \cup \{ \} = A$ .

For any number x, it is always true that x times 1 equals x.

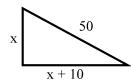
- { } is called the identity element for union.
- 1 is called the identity element for multiplication.

What is the identity element for addition?

1893.  $\{y \mid y \text{ is an integer and } y < -4\} \cup \{z \mid z \text{ is a natural number}\}\$ 

#### The Complete Solutions and Answers

6019. In a right triangle the shortest leg is 10 meters shorter than the other leg. The hypotenuse is 50 meters long. How long is the shorter leg?



We almost always begin a word problem by letting the variable equal the thing we are trying to find out.

Let x = the length of the shorter leg.

Then x + 10 = the length of the longer leg.

By the Pythagorean theorem, 
$$x^2 + (x + 10)^2 = 50^2$$

$$x^2 + x^2 + 20x + 100 = 2500$$

$$2x^2 + 20x - 2400 = 0$$

Divide everything by 2  $x^2 + 10x$ 

 $x^2 + 10x - 1200 = 0$ 

Find two numbers that

multiply to -1200 and add

to 10. 
$$+40$$
 and  $-30$   $(x + 40)(x - 30) = 0$ 

Set each factor equal to zero x + 40 = 0 OR x - 30 = 0

$$x = 30$$
 meters

(x = -40 meters doesn't make any sense for the length of a leg.)

$$6021. \ \frac{5}{y-12} + \frac{17-y}{12-y}$$

The least common multiple is not (y - 12)(12 - y). That's too large. We can make the denominators alike by multiplying the second fraction on the top and bottom by -1.

$$\frac{5}{y-12} + \frac{17-y}{12-y} = \frac{5}{y-12} + \frac{(17-y)(-1)}{(12-y)(-1)}$$

$$= \frac{5+(17-y)(-1)}{y-12}$$

$$= \frac{5-17+y}{y-12}$$

$$= \frac{y-12}{y-12} = 1$$

6025.  $\{x \mid x = a/b \text{ where } a \text{ and } b \text{ are integers and } b \neq 0\}$  is the set of **rational numbers**. All of these are rational numbers: 7/3, -5/8, 200, 4.3238,  $\sqrt{144}$ , and 0, because each of these can be written as an integer divided by a non-zero integer. 200 = 200/1, 4.3238 = 43238/10000,  $\sqrt{144} = 12/1$ , and 0 = 0/83.

# Index

age problems	commutative laws
#68026	#243 35
#612226	#402 35
#557026	#54135
#192828	#501 35
#560037	#22 35
#471644	#4711 37
#4610 44	
	consecutive numbers
area of a rectangle	#704121
#641120	#869521
#7304 20	#627421
#5304 44	#640821
	#833221
cardinality of a set	#9081
#3000 14	#7777 21
#888818	#6124 24
#3700 43	#5231 37
#24549	#6748 38
circumference	continued ratios
#710318	#7020
	#614820
coefficients	#8912 20
#330218	#450324
#570018	#2001 49
#289818	
#427819	
#702332	
#642138	

cube roots and indexes	equations containing fractions
#30351	#8008
#634451	#2566
#650551	#4360 45
#722551	#7803 45
#86753	#4537 48
#2890 57	#2727 48
#64661	#1203 58
#821266	#2108 62
distance = (rate)(time)	
#8870 22	exponents
#52523	#1277 14
#590 23	#9012 33
#6127 23	#8418 33
#930323	#51 33
#8989 23	#5712 33
#44323	#6277 33
#6405 23	#6311 33
#957 24	#6420 33
#979 24	#7788 33
#1100 48	#6742 33
#630353	#6800 33
	#7030 33
distributive property	#7306 33
#6902 21	#9306 33
#8898 22	#7116 37
#52722	#498 58
#35122	#1583 58
#6149 24	#648 62
	#7791 67
division by zero	
#1906 64	
#2444 64	
#692465	

factorials and ordering	factoring—easy trinomials
#131635	#100341
#137535	#1099 41
#160235	#120041
#166735	#1280 41
#80535	#1387 41
#87135	#1520 41
#172536	#407 41
#453137	#873 41
#446837	#522 41
#385048	#54441
	#807 41
factoring—common factors	#951 41
#559240	#4607 44
#491140	#990 58
#510040	
#520140	factoring—grouping
#530240	#260841
#545040	#2800 41
#358 40	#2949 41
#483544	#3009 42
	#3162 42
factoring—difference of squares	#3215 42
#163541	#326042
#168041	#3380 42
#1726 41	#4824 43
#175041	
#1898 41	
#1939 41	
#200041	
#205041	
#231041	
#239041	
#2506 41	
#4030 43	
#412543	

factoring—harder trinomials	fractions—complex
#340742	#1753 47
#350542	#1835 47
#3606 42	#2051 49
#4000 42	
#4260 42	fractions—multiplying and
#4290 42	dividing
#4350 42	#3965 46
#447742	#4401 46
#453342	#5117 46
#483144	#5240 46
#5009 44	
#54749	functions, domains, codomains,
#599 62	images
	#1047 59
fractional and negative exponents	#1122 59
#927551	#869 59
#907351	#644 59
#891951	#1527 59
#100351	#993 59
#8210 52	#1205 60
#122552	#1390 60
	#1263 61
fractions—adding and	#275 62
subtracting	#258 63
#339346	#1140 66
#1060 46	#6955 66
#2954 46	
#322246	
#3900 46	
#3424 46	
#3610 46	
#3870 46	
#602146	
#3960 48	
#3955 48	
#341148	

going from 4 to 11 problems	graphing linear equations
#59313	#1633 31
#91713	#208
#445	#9087 31
#494	#9000 31
#864 13	#470
#532	#530
#980 13	#999 31
#68513	#9011 32
#732 13	#5234 44
#207 14	#997 61
#158514	#255 63
#496554	#2304 66
graphing any equation	graphing points
#570931	#4447 30
#172131	#452030
#615032	#490030
#780032	#91830
#183232	#330330
#277737	#891532
#59558	
	inconsistent and dependent
graphing inequalities in two	equations
dimensions	#1894 34
#1050 64	#1935 34
#1136 64	#2100 34
#3022 64	#2305 34
#1250 64	#5225 34
#1529 64	
#1730 64	integers
#252764	#518
#4180 64	#726 12
#124165	#3116

integers—adding	integers—subtracting
#986 12	#742 12
#188 12	#356 12
#855 12	#521
#240 12	#959
#33312	#585
#97712	#655
#71412	#68212
#46012	#72912
#64012	#98912
#61612	#84012
#944 12	#866 12
#44114	#891 12
#65114	#925
#220318	#91312
#1836 18	#131314
#385543	#90714
#58 49	#5606
integers—multiplying, dividing	job problems
integers—multiplying, dividing #444415	job problems #3430 47
	-
#444415	#3430
#4444	#3430
#4444	#3430 47 #2403
#4444	#3430
#4444	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54
#4444	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58
#4444. 15 #6121. 15 #1409. 16 #1111. 16 #1748. 16 #1830. 16 #3256. 16	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62
#4444. 15 #6121. 15 #1409. 16 #1111. 16 #1748. 16 #1830. 16 #3256. 16 #1625. 16	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63
#4444. 15 #6121. 15 #1409. 16 #1111. 16 #1748. 16 #1830. 16 #3256. 16 #1625. 16 #1371. 16	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63
#4444. 15 #6121. 15 #1409. 16 #1111. 16 #1748. 16 #1830. 16 #3256. 16 #1625. 16 #1371. 16 #1001. 16	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63
#4444. 15 #6121. 15 #1409. 16 #1111. 16 #1748. 16 #1830. 16 #3256. 16 #1625. 16 #1371. 16 #1001. 16 #6181. 18	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63
#4444       15         #6121       15         #1409       16         #1111       16         #1748       16         #1830       16         #3256       16         #1625       16         #1371       16         #1001       16         #6181       18         #5525       18	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63
#4444. 15 #6121. 15 #1409. 16 #1111. 16 #1748. 16 #1830. 16 #3256. 16 #1625. 16 #1371. 16 #1001. 16 #6181. 18 #5525. 18 #9009. 19	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63
#4444       15         #6121       15         #1409       16         #1111       16         #1748       16         #1830       16         #3256       16         #1625       16         #1371       16         #1001       16         #6181       18         #5525       18         #9009       19         #6300       19	#3430. 47 #2403. 47 #2960. 47 #875. 49 #7700. 54 #4177. 58 #1130. 62 #1692. 63

less than <	mean, median, and mode
#136215	averages
#1600 15	#6190 30
#166315	#8900 30
#171715	#8340 30
#192115	#6735 30
#227015	#5222 30
#227515	#5707 30
#333315	#6130 30
#558515	#8977 30
#960 15	#6302 30
#641832	#6417 30
#621538	#4522 32
#36049	#4282 32
#779167	#1222 32
	#5203
linear inequalities	
#230365	mixture problems
#252565	#1850
#263565	#201 27
#289665	#6179 27
#5099 65	#6704 27
#545465	#4507
#560865	#2226
	#5107 44
long division of polynomials	#6323
#301557	#3550 54
#99257	#2892 58
#642 57	#6333 67
#6498 57	
#683157	motion problems
#25157	#1709
#5022 67	#8970
	#906525
	#9225

multiplying binomials and	number, rate, and time problems
trinomials	#8327 25
#2504 39	#920
#2606 39	#1919 26
#2790 39	#2258
#2946 39	#5300 37
#300 39	#7120 38
#321139	#4399 43
#3404 39	#5004 44
#350239	#7333 66
#360139	
#401739	order of operations
#740339	#184422
#7606 39	#8413 22
#435443	#6730 22
	#8000
multiplying by zero	#163022
#293932	#870 24
	#5215 44
natural numbers	
#405 11	ρί π
#589 11	#2249
#6210 32	#2289 17
	#2291
negative and zero exponents	#3299 17
#2500	#4811 17
#1834 36	#6204
#1936 36	#7103
#2308	#8004
#2400 36	#650 57
#260336	
#3370 37	
#730938	
#781453	
#274557	
#1244 66	

polynomials	quadratic equations solved by
#447039	factoring
#471239	#4913 42
#460039	#4829 42
#427539	#4603 42
#482240	#4699 42
#4535 44	#5001
	#4127 43
price and quantity problems	#4020 43
#227226	#6019 43
#2280 28	#5800
	#5597
	#5609 43
principal square roots	#5790 43
#453850	#5101 44
#461150	#1524 58
#471850	
#484851	quadratic equations—completing
#525251	the square
#531151	#1683 55
#559553	#1903 55
#569253	#1942 55
#781565	#5020 55
	#2340 55
proportions	#2410 55
#228416	#2575 55
#3160 16	#2615 55
#1926 16	#4977 55
#4518 18	#1945 56
#4466 19	#2630 58
#6738 32	#596 61
	#5812 66
quadratic equations	
#523644	

quadratic equations—quadratic formula	radical equations
#100955	#4747 52
#101055	#5010
#104455	#4940 52
#59455	#3720 52
#125255	#3979 52
	#7425 52
#49555	#4912 53
#137856	#2301 57
#505056	#277
#561156	#3030 67
#611556	
#632556	radius
#120861	#5566
#230262	#632038
#651167	
	ratio problems
quadratic equations—solving	#154 13
pure quadratics	#718
#261150	#619
#1900 50	
	#511
#206050	#511
#232350	
	#85213
#232350	#852
#232350 #240750	#852
#2323	#852. 13 #326. 13 #39. 13 #467. 13
#2323.       50         #2407.       50         #2570.       50         #4141.       50	#852. 13 #326. 13 #39. 13 #467. 13 #845. 14
#2323.       50         #2407.       50         #2570.       50         #4141.       50         #3620.       50	#852. 13 #326. 13 #39. 13 #467. 13 #845. 14 #1690. 14
#2323.       50         #2407.       50         #2570.       50         #4141.       50         #3620.       50         #3512.       53	#852. 13 #326. 13 #39. 13 #467. 13 #845. 14 #1690. 14 #2930. 14
#2323.       50         #2407.       50         #2570.       50         #4141.       50         #3620.       50         #3512.       53         #6304.       53	#852. 13 #326. 13 #39. 13 #467. 13 #845. 14 #1690. 14 #2930. 14 #6308. 32
#2323.       50         #2407.       50         #2570.       50         #4141.       50         #3620.       50         #3512.       53         #6304.       53         #4300.       53	#852. 13 #326. 13 #39. 13 #467. 13 #845. 14 #1690. 14 #2930. 14 #6308. 32 #5795. 38

rational numbers	repeating decimals
#790 22	#2888 54
#71122	#4330 54
#629 22	#1904 57
#138022	#355561
#6129 24	#8952 66
#303738	
	set builder notation
rationalizing the denominator	#6685
#100752	#7105
#106952	#7792 21
#650952	#8895 21
#24852	#8973
#682552	#941 24
#4860 53	#948 24
#2066 57	
#121262	sets braces
#122067	#492 11
real numbers and irrational	sets and braces
numbers	#221 11
#6290 51	#317 11
#602551	#45 11
#6234 51	#92311
#579951	#699 11
#59761	#900
	#667 14
reflexive property of equality 21	#930 14
#20 21	#9130 66
#161324	
#392743	sets—empty set
#168158	#3711

sets—equality of	slope-intercept form of the line
#50011	#120560
#7111	#99460
#88811	#64560
#40114	#102260
#5349	#139161
#59862	#1260 61
sets—finite and infinite	solving equations
#123 11	#740 24
#560	#5607 54
#63511	#126562
	#581666
sets—is a member of	
#558019	square roots—simplifying
	#52350
simplifying fractions	#3012 50
#311445	#3121 50
#326245	#3716 50
#3508 45	#4321 50
#370545	#4150 50
#93345	#4838 53
#2950 45	#1040 57
#3858 48	#2522 62
	#800965
slope	
#125860	symmetric property of equality
#289460	#204 22
#574060	#526654
#251163	#1125 62
#2072 63	
#1049 63	transposing
	#1930 30
	#2294 30
	#2901 30

trapezoid—area of	union of sets
#8950 20	#924 29
#9122 20	#3328 29
#4123 24	#4280 29
	#4500 29
two equations solved by	#800
elimination	#600
#401029	#1893 29
#189129	#950 32
#229229	#3005 37
#2904 29	#5111 44
#4505 29	
#4519 29	volume
#293532	#2717 36
#641432	#2788 36
#470037	#2943 36
#428437	#3366 36
#429543	#4450 36
#168558	#4820 37
#510466	#7790 38
two equations solved by graphing	whole numbers
#2300	#347 12
#2909	#5590 37
#481837	
	word problems in two unknowns
two equations solved by	#6207 31
substitution	#6305 31
#558834	#8207 32
#631534	
#690234	
#4000	